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MATHS METHODS

PODCAST

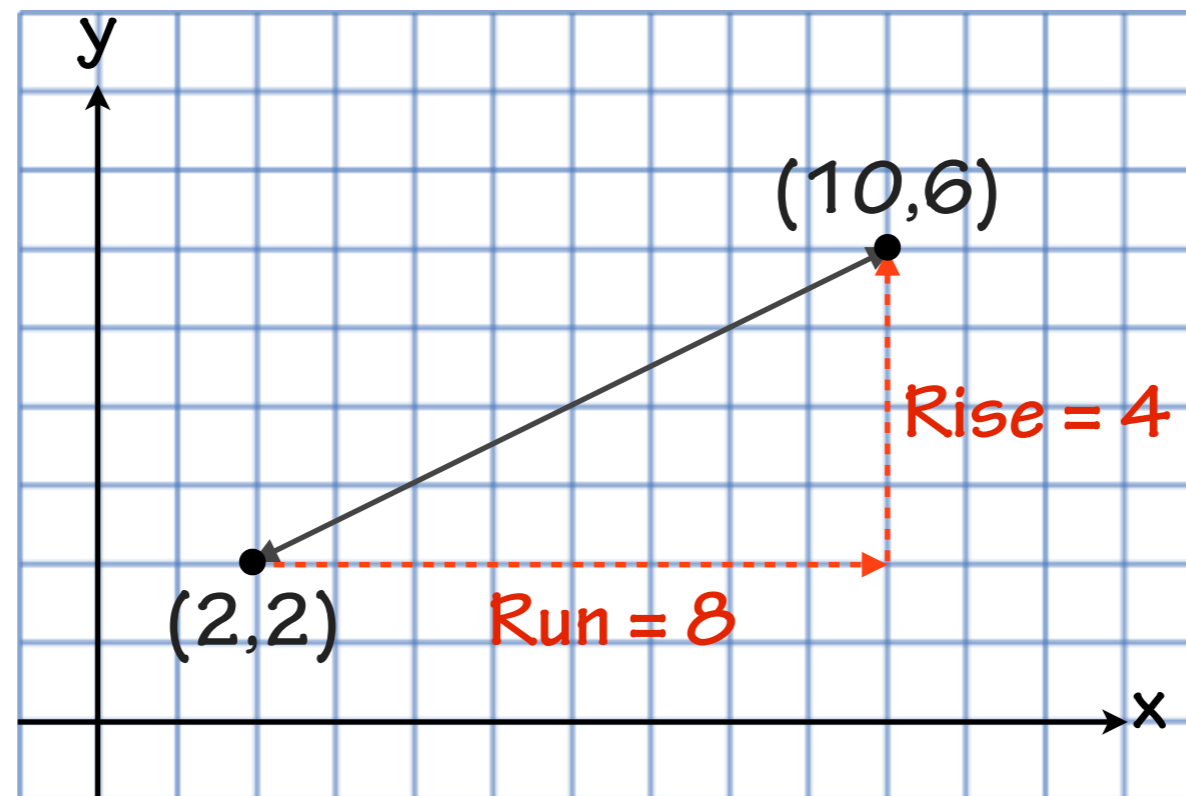


Linear Graphs

- *Gradient of lines*
- *Graphing linear equations*
- *Finding the equation of a line*
- *Perpendicular lines*
- *Distance between points*
- *Midpoint of a line*

Gradient of lines

The gradient is the measure of how far up a line rises, as it runs across.



Gradient of 4/8:
Same as 1/2.

$$\text{gradient} = \frac{\text{rise}}{\text{run}} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\text{gradient} = \frac{6 - 2}{10 - 2} = \frac{4}{8} = \frac{1}{2}$$

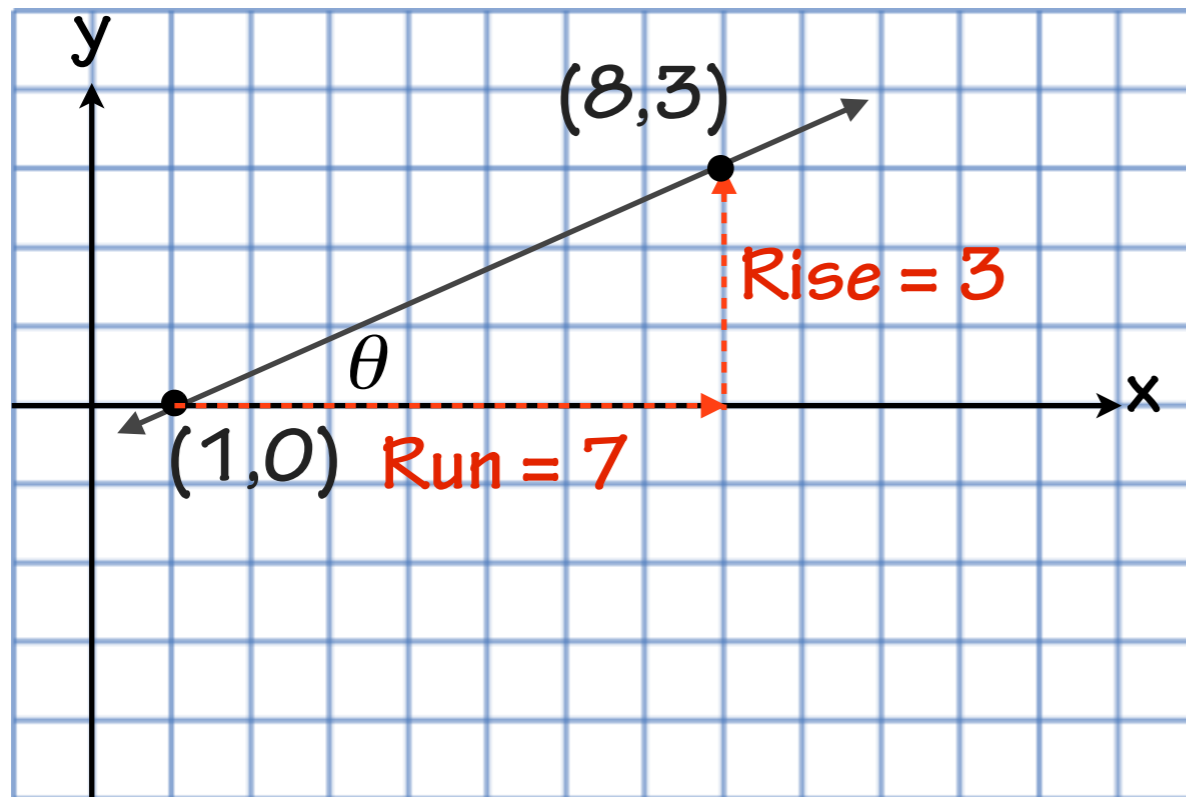
Positive gradient

Negative gradient

Angles & gradients

The gradient of the line can be used to find the angle between the line and the axis.

$$\text{gradient} = \frac{\text{rise}}{\text{run}} = \frac{\text{opposite}}{\text{adjacent}} = \tan\theta$$



$$\tan\theta = \frac{3}{7}$$

$$\theta = \tan^{-1}\left(\frac{3}{7}\right)$$

$$\theta \approx 23.2^\circ$$

- Negative gradient: use a negative angle (Clockwise, below the axis) or the supplementary angle ($180^\circ - \theta$)

Angles & gradients

Find the acute angle between the two lines:

$$y = \frac{-2x}{3} + 10$$

$$m = -\frac{2}{3}$$

$$\theta = \tan^{-1}\left(\frac{-2}{3}\right)$$

$$\theta = -33.69^\circ$$

$$\theta = 146.31^\circ$$

$$y = 3x + 2$$

$$m = 3$$

$$\theta = \tan^{-1}(3)$$

$$\theta = 71.57^\circ$$

$$\theta_3 = 180^\circ - 33.69^\circ - 71.57^\circ$$

$$\theta_3 = 74.74^\circ$$

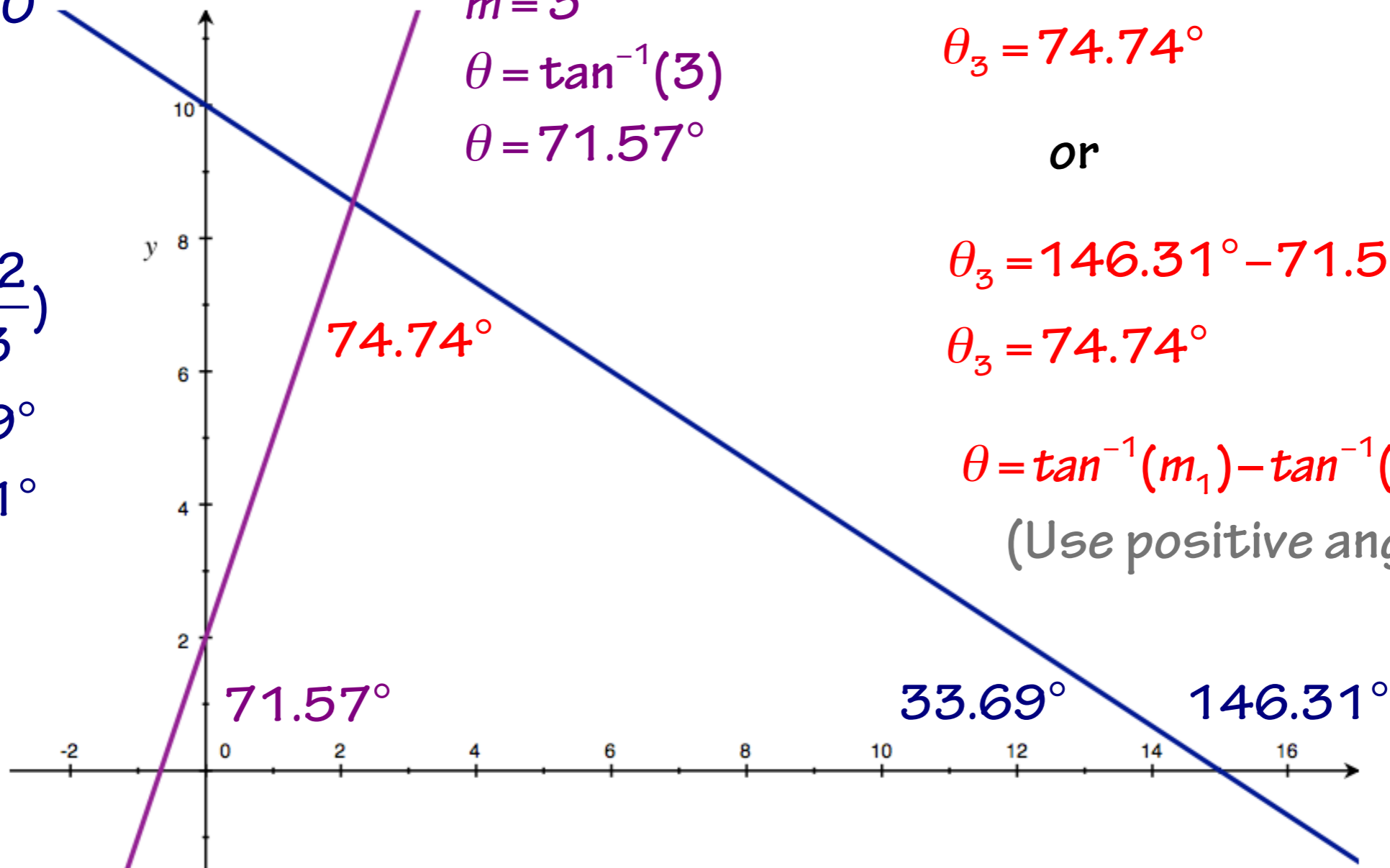
or

$$\theta_3 = 146.31^\circ - 71.57^\circ$$

$$\theta_3 = 74.74^\circ$$

$$\theta = \tan^{-1}(m_1) - \tan^{-1}(m_2)$$

(Use positive angles)



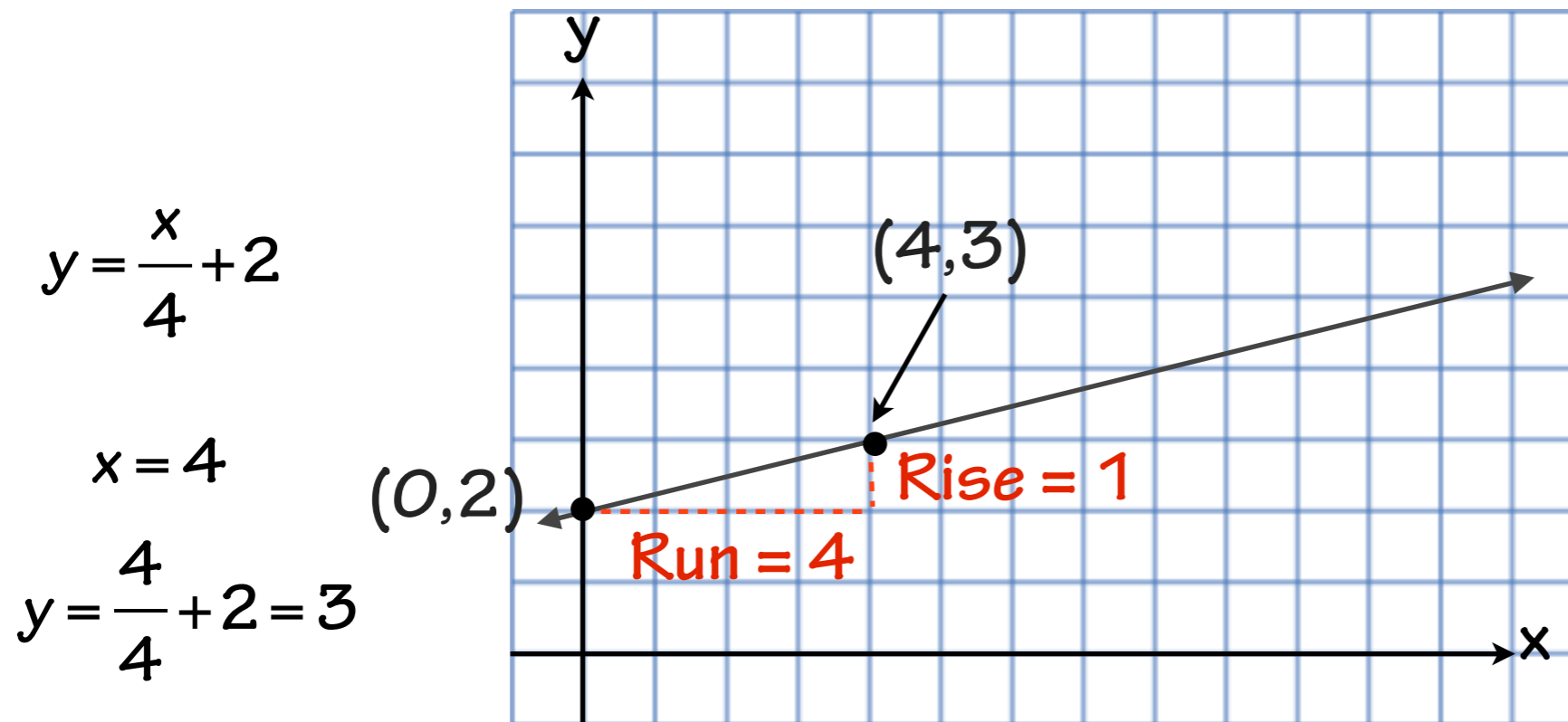
Graphing equations - gradient form

Linear equations are defined by a gradient and y-intercept

$$y = mx + c$$

$m = \text{gradient}$ (indicated by a red arrow pointing to m)

$c = \text{y intercept}$ (indicated by a blue arrow pointing to c)



Graphing equations - intercept form

- Linear equations can also be written in an intercept form.
- The gradient form ($y = mx + c$) can be rearranged.

$$\frac{x}{a} + \frac{y}{b} = 1 \quad bx + ay = ab$$

$$y = \frac{x}{2} - 4 \rightarrow 4 = \frac{x}{2} - y \rightarrow \frac{x}{8} - \frac{y}{4} = 1 \rightarrow x - 2y = 8$$

x intercept: $y = 0$ y intercept: $x = 0$

$$x - 2y = 8$$

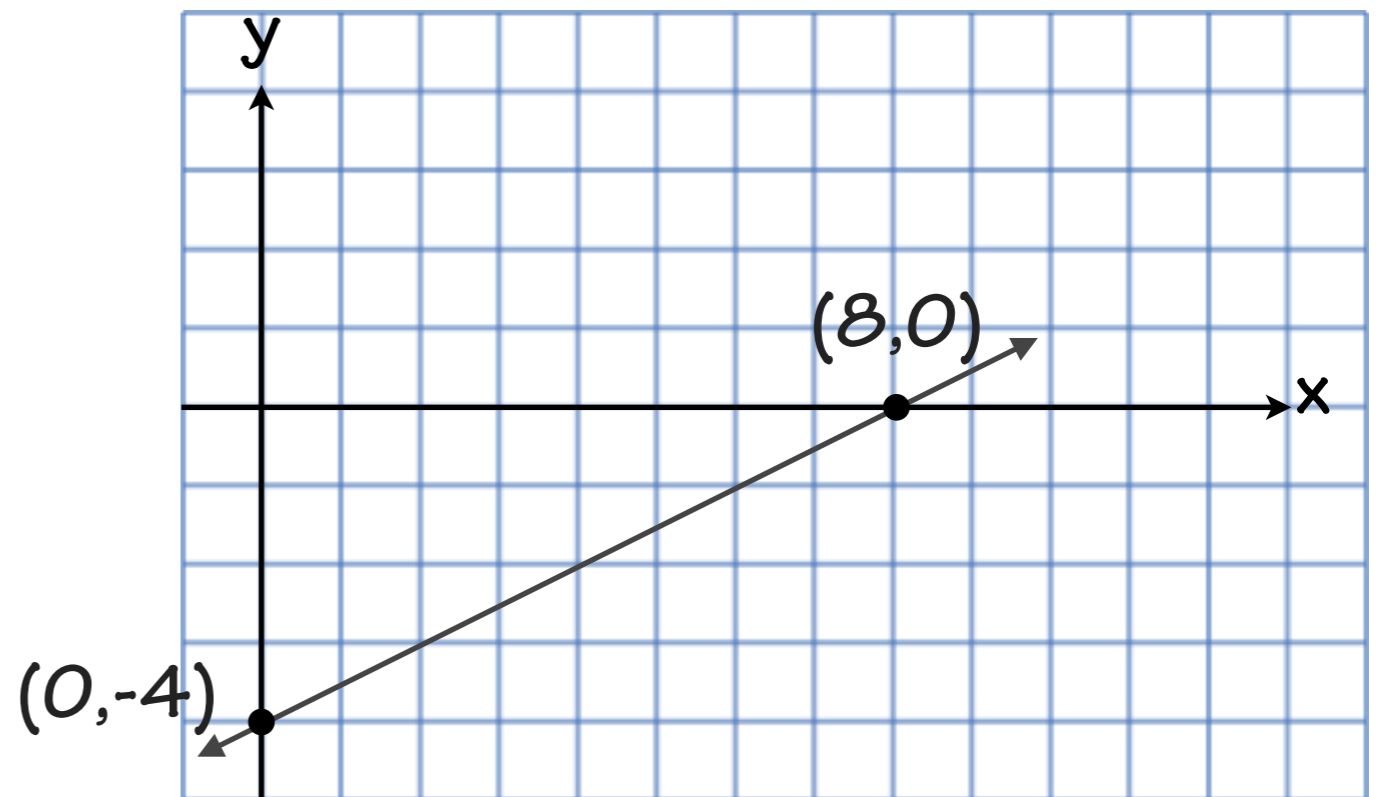
$$x - 2 \times 0 = 8$$

$$x = 8$$

$$0 - 2y = 8$$

$$y = \frac{8}{-2}$$

$$y = -4$$



Finding the equation of a line - two points

- To find the equation of a line, a point and a gradient are needed.
- If two points are given, the gradient must be found first.
- The rule $y - y_1 = m(x - x_1)$ is used to find the linear equation.

Gradient:

$$m = \frac{-2 - 2}{9 - 1} = \frac{-4}{8} = -\frac{1}{2}$$

Equation:

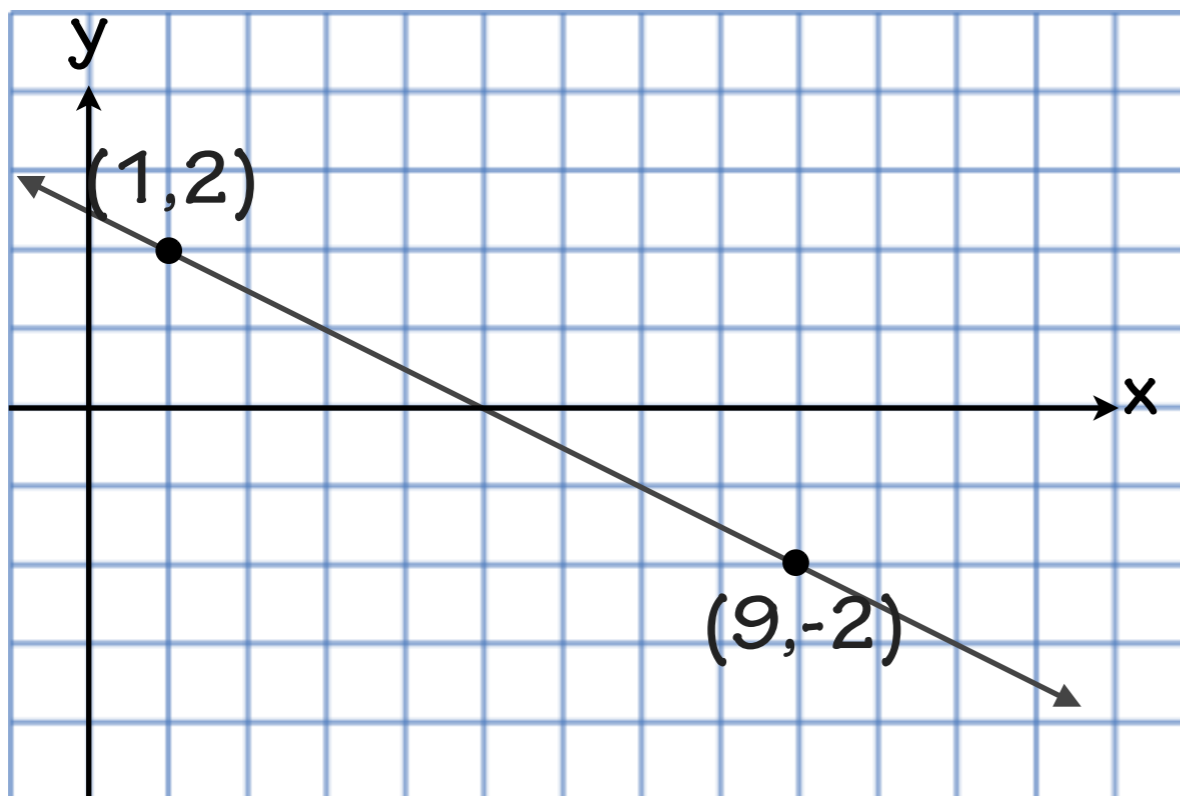
$$y - y_1 = m(x - x_1)$$

$$y - 2 = -\frac{1}{2}(x - 1)$$

$$y - 2 = -\frac{1}{2}x + \frac{1}{2}$$

$$y = -\frac{1}{2}x + \left(\frac{1}{2} + 2\right)$$

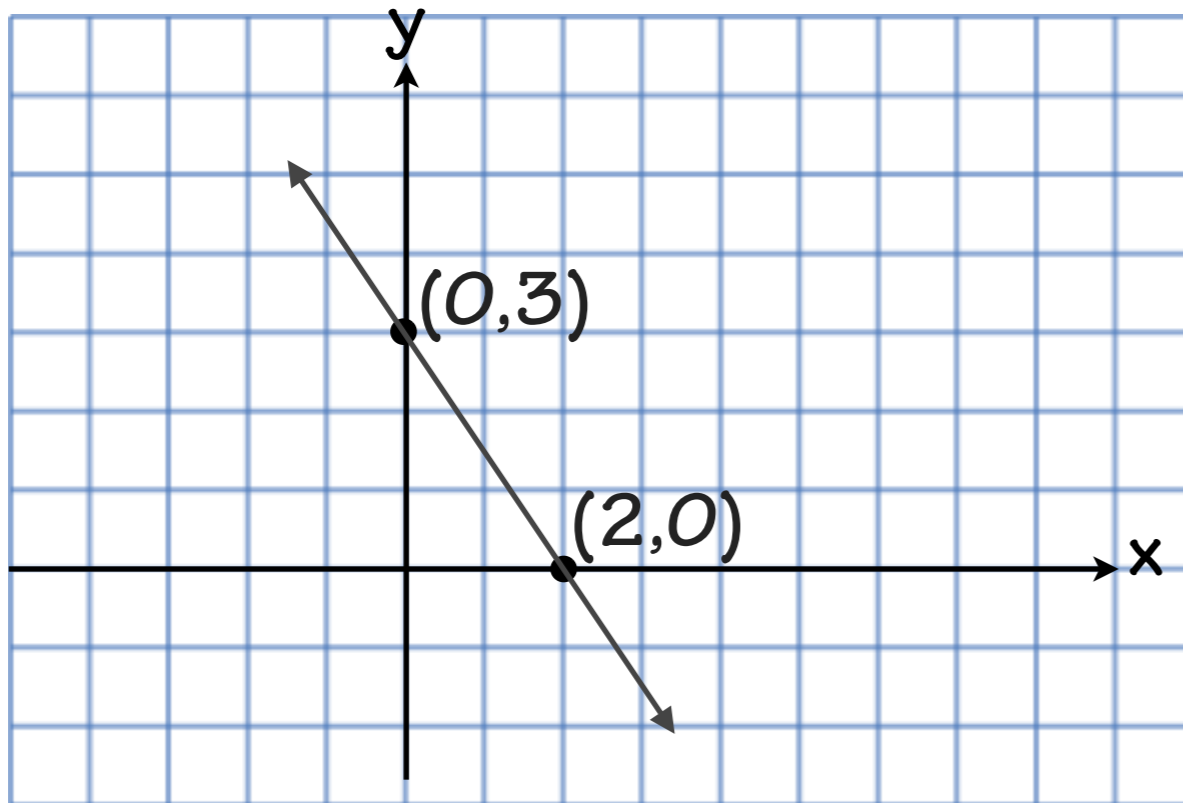
$$y = -\frac{1}{2}x + \left(\frac{1}{2} + \frac{4}{2}\right)$$



$$y = -\frac{1}{2}x + \frac{5}{2}$$

Finding the equation of a line - two intercepts

- To find the equation of a line, the two axis intercepts can be used.
- The graph of the function $x + y = 1$ can be transformed through dilations & reflections.



$$\frac{x}{a} + \frac{y}{b} = 1$$

x intercept y intercept

$$\frac{x}{2} + \frac{y}{3} = 1$$

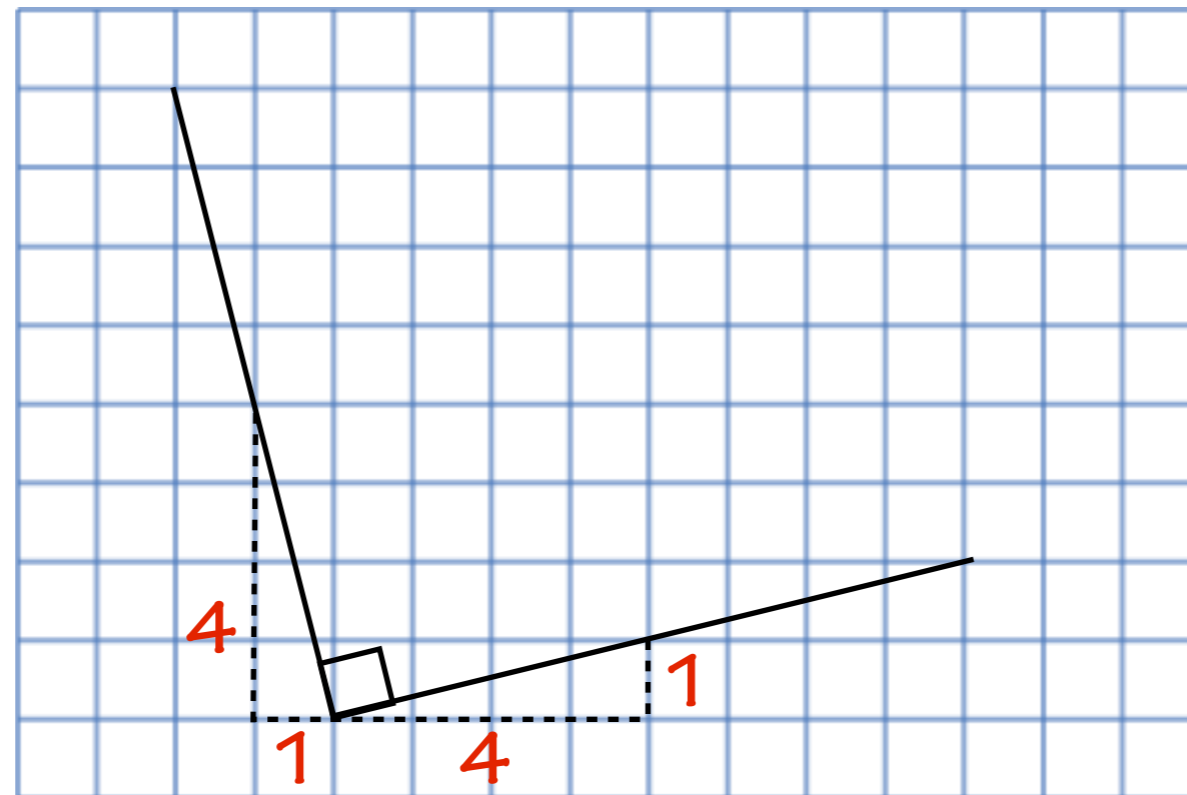
or

$$3x + 2y = 6$$

Perpendicular lines

Two lines are perpendicular if they cross at a 90° angle.

Gradient of $-4/1$:



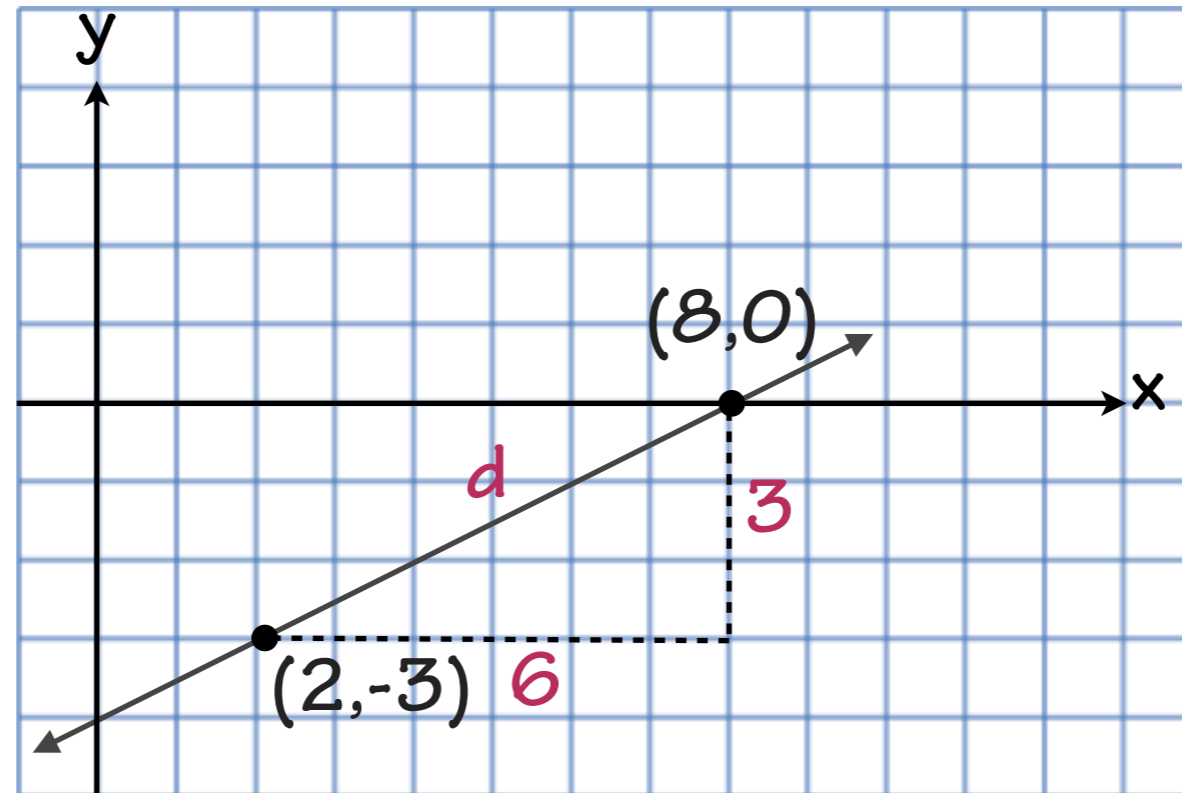
Gradient of $1/4$:

Two lines are perpendicular if their gradients multiply to -1 .

$$m_1 \times m_2 = -1 \quad m_2 = -\frac{1}{m_1}$$

Distance between points

The distance between two points can be found using Pythagoras' theorem:



$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$d^2 = 6^2 + 3^2$$

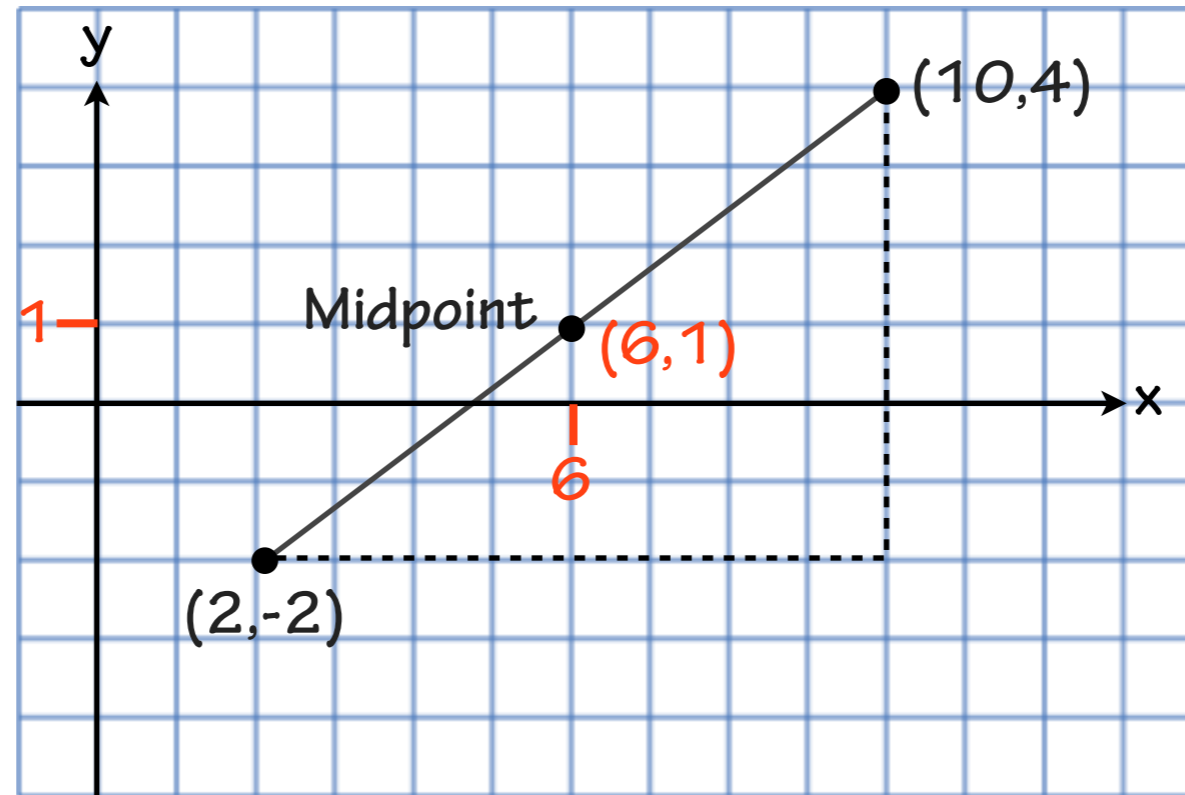
$$d^2 = 36 + 9$$

$$d^2 = 45$$

$$d = \sqrt{45} = 6.7$$

Midpoint of a segment

The midpoint of a straight line segment is at the middle of the x & y values.



x value:

$$x_m = \frac{x_1 + x_2}{2}$$
$$x_m = \frac{2 + 10}{2} = \frac{12}{2} = 6$$

y value:

$$y_m = \frac{y_1 + y_2}{2}$$
$$y_m = \frac{-2 + 4}{2} = \frac{2}{2} = 1$$

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